

# NOMBRES - Curiosités, théorie et usages

## NOMBRES somme chiffres puissances

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### Définition

Un nombre et ses puissances successives. La somme des chiffres de ces puissances. Quels sont ceux dont cette somme se répètent plusieurs fois.

**Exemple** avec le nombre 19 qui présente trois fois la même somme:

$$19 \text{ et } 1 + 9 = 10;$$

$$19^2 = 361 \text{ et } 3 + 6 + 1 = 10;$$

$$19^4 = 130\,321 \text{ et } 1 + 3 + 0 + 3 + 2 + 1 = 10$$

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### Table des sommes des chiffres des puissances

Nombres ressentant au moins deux fois la même somme. Les sommes répétées sont en jaune.

#### Exemples

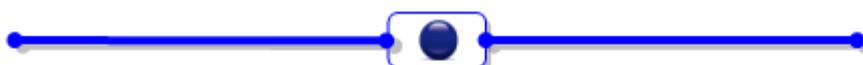
$2^3 = 8$	8	$3^2 = 9$	9	$4^2 = 16$	$1 + 6 = 7$
$2^9 = 512$	$5 + 1 + 2 = 8$	$3^3 = 27$	$2 + 7 = 9$	$4^5 = 1024$	$1 + 0 + 2 + 4 = 7$
		$3^4 = 81$	$8 + 1 = 9$		
		$3^5 = 243$	$2 + 4 + 3 = 9$		

Pour les nombres de 2 à 100 et les puissances de 1 à 10 (s1 à s10)

n	s1	s2	s3	s4	s5	s6	s7	s8	s9	s10
2	[2	4	8	7	5	10	11	13	8	7]
3	[3	9	9	9	9	18	18	18	27	27]
4	[4	7	10	13	7	19	22	25	19	31]
6	[6	9	9	18	27	27	36	36	36	36]
7	[7	13	10	7	22	28	25	31	28	43]
8	[8	10	8	19	26	19	26	37	35	37]
9	[9	9	18	18	27	18	45	27	45	45]
12	[3	9	18	18	27	45	36	54	45	45]
15	[6	9	18	18	36	27	45	45	54	54]

17	[8	19	17	19	35	37	35	55	71	55]
18	[9	9	18	27	45	18	18	45	63	54]
19	[10	10	28	10	37	37	55	46	73	46]
21	[3	9	18	27	18	36	36	54	54	72]
24	[6	18	18	27	36	36	45	36	45	63]
26	[8	19	26	37	35	46	35	55	71	64]
27	[9	18	27	18	36	45	27	54	81	63]
28	[10	19	19	28	28	37	46	64	64	82]
33	[6	18	27	27	36	54	54	45	54	81]
36	[9	18	27	36	36	45	54	54	72	72]
37	[10	19	19	28	46	46	55	55	82	82]
39	[12	9	27	18	36	45	45	45	72	54]
42	[6	18	27	27	27	45	45	72	72	72]
44	[8	19	26	37	35	46	62	46	62	82]
45	[9	9	18	18	36	45	54	54	72	63]
46	[10	10	28	37	46	64	55	46	64	82]
48	[12	9	18	27	45	36	54	63	72	63]
51	[6	9	18	27	27	54	63	63	54	54]
53	[8	19	35	37	44	37	53	55	71	82]
54	[9	18	27	27	36	54	63	54	54	72]
55	[10	10	28	28	37	46	46	73	82	64]
57	[12	18	27	18	36	54	72	36	72	72]
58	[13	16	19	31	52	55	58	52	91	76]
63	[9	27	18	36	45	36	72	63	72	99]
64	[10	19	19	37	37	64	46	73	82	82]
66	[12	18	36	45	36	45	45	63	81	99]
67	[13	25	19	13	25	55	40	70	82	85]
69	[15	18	27	27	36	45	63	72	81	81]
71	[8	10	26	28	35	37	53	64	71	64]
72	[9	18	27	45	45	45	36	54	99	81]
73	[10	19	28	37	37	46	64	64	91	100]
75	[12	18	27	27	45	63	72	45	99	81]
78	[15	18	27	27	54	45	72	54	81	90]
81	[9	18	18	27	45	54	72	63	81	90]
82	[10	19	28	28	46	37	73	73	73	82]
84	[12	18	27	45	36	45	63	81	81	99]
87	[15	27	27	45	45	36	81	54	72	90]
91	[10	19	28	46	28	55	55	55	82	73]
93	[12	27	27	27	63	63	54	72	81	99]
96	[15	18	36	45	54	81	63	90	90	90]
99	[18	18	36	36	54	45	72	72	90	72]

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## Cas des sommes répétées plus de deux fois pour n de 10 à 1000

Nombre, [somme répétée, quantité de fois], [les sommes pour les puissances de 1 à 10 pour localiser le triplet]

**Exemple:** avec n = 12, un triplet concerne la somme 45; elle est obtenue pour les puissances (6, 9 et 10)

12, [45, 3], [3, 9, 18, 18, 27, 45, 36, 54, 45, 45]  
18, [18, 3], [9, 9, 18, 27, 45, 18, 18, 45, 63, 54]  
19, [10, 3], [10, 10, 28, 10, 37, 37, 55, 46, 73, 46]  
24, [36, 3], [6, 18, 18, 27, 36, 36, 45, 36, 45, 63]  
33, [54, 3], [6, 18, 27, 27, 36, 54, 54, 45, 54, 81]  
39, [45, 3], [12, 9, 27, 18, 36, 45, 45, 45, 72, 54]  
42, [27, 3], [6, 18, 27, 27, 27, 45, 45, 72, 72, 72]  
42, [72, 3], [6, 18, 27, 27, 27, 45, 45, 72, 72, 72]  
51, [54, 3], [6, 9, 18, 27, 27, 54, 63, 63, 54, 54]  
54, [54, 3], [9, 18, 27, 27, 36, 54, 63, 54, 54, 72]  
57, [72, 3], [12, 18, 27, 18, 36, 54, 72, 36, 72, 72]  
66, [45, 3], [12, 18, 36, 45, 36, 45, 45, 63, 81, 99]  
72, [45, 3], [9, 18, 27, 45, 45, 45, 36, 54, 99, 81]  
82, [73, 3], [10, 19, 28, 28, 46, 37, 73, 73, 73, 82]  
91, [55, 3], [10, 19, 28, 46, 28, 55, 55, 55, 82, 73]  
93, [27, 3], [12, 27, 27, 27, 63, 63, 54, 72, 81, 99]  
96, [90, 3], [15, 18, 36, 45, 54, 81, 63, 90, 90, 90]  
99, [72, 3], [18, 18, 36, 36, 54, 45, 72, 72, 90, 72]  
105, [45, 3], [6, 9, 27, 27, 45, 45, 45, 81, 81, 99]  
117, [45, 3], [9, 27, 18, 45, 45, 54, 45, 63, 81, 117]  
141, [72, 3], [6, 27, 18, 36, 45, 72, 72, 81, 72, 90]  
147, [63, 3], [12, 18, 27, 54, 54, 63, 63, 63, 90, 90]  
156, [99, 3], [12, 18, 36, 45, 72, 54, 72, 99, 99, 99]  
165, [81, 3], [12, 18, 27, 27, 36, 54, 81, 81, 81, 108]  
189, [54, 3], [18, 18, 36, 54, 54, 54, 81, 63, 90, 108]  
204, [45, 3], [6, 18, 45, 45, 45, 72, 72, 108, 99, 90]  
219, [27, 3], [12, 27, 27, 27, 63, 54, 63, 81, 108, 99]  
249, [72, 3], [15, 9, 36, 27, 72, 54, 72, 81, 108, 72]  
253, [64, 3], [10, 19, 37, 37, 64, 64, 64, 91, 91, 109]  
262, [55, 3], [10, 28, 46, 55, 55, 55, 64, 91, 100, 100]  
267, [27, 3], [15, 27, 27, 27, 54, 63, 81, 81, 108, 108]  
333, [63, 3], [9, 27, 36, 36, 63, 63, 90, 63, 108, 135]  
336, [108, 3], [12, 27, 36, 45, 54, 81, 99, 108, 108, 108]  
339, [72, 3], [15, 18, 45, 36, 72, 72, 81, 72, 108, 108]  
357, [81, 3], [15, 27, 45, 36, 81, 81, 90, 81, 117, 99]  
379, [82, 3], [19, 19, 46, 46, 82, 73, 73, 82, 82, 109]  
387, [36, 3], [18, 36, 36, 36, 54, 54, 90, 81, 117, 135]  
**414, [63, 4], [9, 27, 45, 63, 63, 63, 63, 108, 108, 108]**  
**Seul cas avec quatre fois la même somme des chiffres**  
414, [108, 3], [9, 27, 45, 63, 63, 63, 63, 108, 108, 108]  
417, [81, 3], [12, 36, 27, 36, 72, 81, 81, 90, 81, 117]

444, [63, 3], [12, 27, 45, 54, 63, 63, 81, 63, 90, 135]  
 468, [18, 3], [18, 18, 18, 54, 72, 63, 90, 90, 108, 108]  
 478, [73, 3], [19, 28, 28, 46, 73, 73, 73, 91, 109, 91]  
 483, [90, 3], [15, 27, 45, 45, 72, 90, 90, 90, 99, 153]  
 486, [90, 3], [18, 27, 36, 54, 45, 63, 90, 90, 90, 126]  
 585, [18, 3], [18, 18, 18, 45, 45, 63, 81, 117, 117, 135]  
 595, [73, 3], [19, 19, 37, 37, 73, 73, 73, 91, 127, 109]  
 627, [99, 3], [15, 27, 45, 36, 63, 99, 72, 99, 99, 126]  
 681, [81, 3], [15, 27, 27, 36, 63, 81, 81, 108, 81, 126]  
 684, [63, 3], [18, 36, 18, 63, 63, 63, 90, 135, 117, 117]  
 685, [28, 3], [19, 28, 28, 28, 73, 64, 91, 109, 100, 109]  
 693, [90, 3], [18, 27, 36, 27, 90, 90, 108, 90, 144, 144]  
 712, [109, 3], [10, 28, 37, 55, 64, 73, 100, 109, 109, 109]  
 771, [108, 3], [15, 27, 27, 36, 54, 63, 108, 90, 108, 108]  
 795, [117, 3], [21, 18, 45, 54, 72, 81, 72, 117, 117, 117]  
 822, [72, 3], [12, 36, 36, 72, 72, 72, 90, 108, 117, 117]  
 846, [81, 3], [18, 27, 45, 54, 81, 81, 81, 108, 144, 144]  
 849, [108, 3], [21, 18, 36, 45, 54, 63, 108, 108, 117, 108]  
 856, [109, 3], [19, 28, 28, 55, 73, 73, 109, 109, 109, 118]  
 883, [109, 3], [19, 46, 55, 55, 82, 109, 91, 109, 109, 172]

**Commentaires:** seul 414 présente un quadruplet jusqu'à 10 000 au moins pour les dix puissances de 1 à 10.

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### Quels sont les nombres et ses puissances associées à une somme donnée

Somme, quantité de  $n^k$  ayant cette somme de chiffres pour  $n$  de 2 à 100 et les puissances de 2 à 5; liste des nombres et puissances

**Exemple:** avec la somme 4 on trouve:  $2^2 = 4$  et  $11^2 = 121 \Rightarrow 1 + 2 + 1 = 4$

Avec 5, une seule occurrence avec  $2^5 = 32 \Rightarrow 3 + 2 = 5$

Avec 6, aucune possibilité pour  $n^k$  avec  $n$  jusqu'à 100 et  $k$  de 2 à 5.

### Liste

4	2	[2, 2], [11, 2]
5	1	[2, 5]
7	7	[2, 4], [4, 2], [4, 5], [5, 2], [7, 4], [32, 2], [49, 2]
8	4	[2, 3], [5, 3], [8, 3], [11, 3]
9	15	[3, 2], [3, 3], [3, 4], [3, 5], [6, 2], [6, 3], [9, 2], [12, 2], [15, 2], [18, 2], [21, 2], [39, 2], [45, 2], [48, 2], [51, 2]
10	9	[4, 3], [7, 3], [8, 2], [19, 2], [19, 4], [35, 2], [46, 2], [55, 2], [71, 2]
11	1	[5, 5]
13	15	[4, 4], [5, 4], [7, 2], [16, 2], [25, 2], [29, 2], [34, 2], [38, 2], [47, 2], [52, 2], [56, 2], [61, 2], [65, 2], [67, 4], [79, 2]

14	1	[11, 5]
16	12	[11, 4], [13, 2], [14, 2], [22, 2], [23, 2], [31, 2], [41, 2], [58, 2], [59, 2], [68, 2], [85, 2], [95, 2]
17	6	[14, 3], [17, 3], [23, 3], [47, 3], [68, 3], [74, 3]
18	36	[6, 4], [9, 3], [9, 4], [12, 3], [12, 4], [15, 3], [15, 4], [18, 3], [21, 3], [21, 5], [24, 2], [24, 3], [27, 2], [27, 4], [33, 2], [36, 2], [39, 4], [42, 2], [45, 3], [45, 4], [48, 3], [51, 3], [54, 2], [57, 2], [57, 4], [63, 3], [66, 2], [69, 2], [72, 2], [75, 2], [78, 2], [81, 2], [81, 3], [84, 2], [96, 2], [99, 2]
19	28	[8, 4], [13, 3], [16, 3], [17, 2], [17, 4], [22, 3], [25, 3], [26, 2], [28, 2], [28, 3], [34, 3], [35, 4], [37, 2], [37, 3], [44, 2], [52, 3], [53, 2], [58, 3], [62, 2], [64, 2], [64, 3], [67, 3], [73, 2], [82, 2], [85, 3], [89, 2], [91, 2], [98, 2]
22	14	[7, 5], [13, 4], [14, 4], [22, 4], [31, 4], [43, 2], [52, 5], [59, 4], [74, 2], [77, 4], [85, 4], [88, 2], [92, 2], [97, 2]
23	1	[29, 5]
25	15	[13, 5], [16, 4], [22, 5], [25, 4], [29, 4], [34, 4], [38, 4], [43, 4], [52, 4], [67, 2], [67, 5], [76, 2], [77, 2], [86, 2], [94, 2]
26	16	[8, 5], [26, 3], [29, 3], [32, 3], [35, 3], [38, 3], [41, 3], [44, 3], [56, 3], [59, 3], [62, 3], [65, 3], [71, 3], [77, 3], [86, 3], [98, 3]
27	35	[6, 5], [9, 5], [12, 5], [18, 4], [21, 4], [24, 4], [27, 3], [33, 3], [33, 4], [36, 3], [39, 3], [42, 3], [42, 4], [42, 5], [48, 4], [51, 4], [51, 5], [54, 3], [54, 4], [57, 3], [63, 2], [69, 3], [69, 4], [72, 3], [75, 3], [75, 4], [78, 3], [78, 4], [81, 4], [84, 3], [87, 2], [87, 3], [93, 2], [93, 3], [93, 4]
28	22	[19, 3], [28, 4], [28, 5], [31, 3], [37, 4], [43, 3], [46, 3], [49, 3], [55, 3], [55, 4], [61, 3], [71, 4], [73, 3], [79, 3], [82, 3], [82, 4], [88, 3], [89, 4], [91, 3], [91, 5], [94, 3], [97, 3]
29	4	[14, 5], [23, 5], [32, 5], [41, 5]
31	13	[16, 5], [23, 4], [32, 4], [34, 5], [41, 4], [43, 5], [49, 4], [58, 4], [68, 4], [76, 4], [83, 2], [86, 4], [95, 4]
32	3	[47, 5], [65, 5], [74, 5]
34	7	[31, 5], [61, 4], [65, 4], [79, 4], [83, 4], [85, 5], [94, 5]
35	10	[17, 5], [26, 5], [35, 5], [44, 5], [53, 3], [62, 5], [71, 5], [83, 3], [89, 3], [95, 3]
36	18	[15, 5], [24, 5], [27, 5], [33, 5], [36, 4], [36, 5], [39, 5], [45, 5], [54, 5], [57, 5], [63, 4], [66, 3], [66, 5], [69, 5], [84, 5], [96, 3], [99, 3], [99, 4]
37	13	[19, 5], [26, 4], [44, 4], [46, 4], [53, 4], [55, 5], [62, 4], [64, 4], [64, 5], [73, 4], [73, 5], [76, 3], [98, 4]
38	1	[86, 5]
40	2	[25, 5], [61, 5]
41	4	[38, 5], [56, 5], [83, 5], [92, 5]
43	6	[47, 4], [49, 5], [56, 4], [76, 5], [92, 4], [97, 4]
44	2	[53, 5], [92, 3]
45	12	[18, 5], [48, 5], [63, 5], [66, 4], [72, 4], [72, 5], [75, 5], [81, 5], [84, 4], [87, 4], [87, 5], [96, 4]
46	4	[37, 5], [46, 5], [82, 5], [91, 4]
47	3	[59, 5], [68, 5], [77, 5]
49	4	[79, 5], [88, 5], [94, 4], [97, 5]
52	3	[58, 5], [74, 4], [88, 4]
53	2	[89, 5], [98, 5]
54	3	[78, 5], [96, 5], [99, 5]

<b>56</b>	<b>1</b>	<b>[95, 5]</b>
<b>63</b>	<b>1</b>	<b>[93, 5]</b>

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